$$P_i x = A_i (A_i^T A_i)^{-1} A_i^T x.$$